ALAGAPPA UNIVERSITY, KARAIKUDI NEW SYLLABUS UNDER CBCS PATTERN (w.e.f.2017-18)

G	Course	Norma of the Comme	Cr	Hrs./	Max. Marks		
Sem.	Code	Name of the Course	Cr.	Week	Int.	Ext.	Total
	7MMA1C1	Core–I – Algebra – I		6	25	75	100
	7MMA1C2	Core–II – Analysis – I		6	25	75	100
	7MMA1C3	Core – III –Differential Geometry	5	6	25	75	100
	7MMA1C4	Core –IV –Ordinary Differential	5	6	25	75	100
		Equations					
Ι		Elective–I: (Choose One out of Three)					
	7MMA1E1	A) Number Theory (or)					
	7MMA1E2	B) Calculus of Variations and	4	6	25	75	100
		Special Functions (or)		Ū	20	15	100
	7MMA1E3	C) Data Structures and Algorithms					
		Theory and Practical		20			
		Total	24	30			500
	/MMA2C1	Core – V–Algebra – II	5	6	25	/5	100
	/MMA2C2	Core – VI–Analysis – II	2	6	25	/5	100
	7MMA2C3	Core–VII –Partial Differential	5	6	25	75	100
п		Equations	~		25	75	100
11	/MMA2C4	Core – VIII–Mechanics	3	6	25	/5	100
	71111 4 2 5 1	Liective – II :(Choose One out of Three)	4	6	25	75	100
	7 MMA2E1	B) Applied Algebra					
	7MMA2E2	C) Difference Equations					
	71011017 (22.5	Total	24	30			500
	7MMA3C1	Core–IX –Complex Analysis	5	6	25	75	100
	7MMA3C2	Core–X –Topology – I	5	6	25	75	100
	7MMA3C3	Core-XI -Probability and Statistics	5	6	25	75	100
	///////////////////////////////////////	Elective-III (Choose One out of Three)	5	6	25	75	100
	7MMA3E1	A) Discrete Mathematics (or)					
III	7MMA3E2	B) Fluid Dynamics (or)	4				
	7MMA3E3	C) Automata Theory					
		Elective–IV:(Choose One out of Three)			25	75	100
	7MMA3E4	A) Fuzzy Mathematics (or)	4	6			
	7MMA3E5	B) Stochastic Processes (or)	4				
	7MMA3E6	C) Combinatorial Mathematics					
		Total	23	30			500
IV	7MMA4C1	Core – XII –Functional Analysis	5	8	25	75	100
	7MMA4C2	Core – XIII–Operations Research	5	8	25	75	100
	7MMA4C3	Core – XIV–Topology II	5	7	25	75	100
		Elective-V:(Choose One out of Three)					
	7MMA4E1	A) Advanced Statistics	4	7	25	75	100
	7MMA4E2	B) Stochastic Differential Equations	4				100
	7MMA4E3	C) Numerical Methods					40.0
		Total	19	30			400
		Grand Total	90	120			1900

M.Sc., MATHEMATICS – PROGRAMME STRUCTURE

M.Sc. MATHEMATICS

I YEAR – I SEMESTER COURSE CODE: 7MMA1C1

CORE COURSE-I -ALGEBRA-I

Unit I

Group Theory: Definition of a group – Some examples of groups – Some preliminary Lemmas – Subgroups – A counting principle – Normal subgroups and Quotient groups – Homomorphisms – Automorphisms – Cayley's Theorem – Permutation Groups.

Unit II

Another counting Principle – Sylow's Theorem – Direct products

Unit III

Ring Theory: Definition and examples of rings – some special classes of Rings – Homomorphisms.

Unit IV

Ideals and Quotient Rings – More ideals and Quotient Rings – The field of quotients of an Integral Domain

Unit V

Enclidean Rings – A Particular Euclidean Ring – Polynomial Rings – Polynomials over the Rational Field – Polynomial Rings over commutative Rings.

Text Book(s)

I.N.Herstein, Topics in Algebra (2nd Edition) Wiley Eastern Limited, New Delhi, 1975.

Chapter II – 2.1 to 2.13 & Chapter III

Books for Supplementary Reading and Reference:

- 1. M.Artin, Algebra, Prentice Hall of India, 1991.
- 2. John B.Fraleigh, A First Course in Abstract Algebra, Addison Wesley, Mass, 1982.
- 3. D.S.Malik, J.N.Mordeson and M.K.Sen, Fundamentals of Abstract Algebra, McGraw Hill (International Edition), New York, 1997.

CORE COURSE-II – ANALYSIS – I

Unit I

Basic Topology: Metric Spaces – Compact sets – Perfect sets – Connected sets.

Unit II

Numerical sequences and series; Convergent sequences, Subsequences, Cauchy sequences, Upper and Lower limits – Special sequences, Series, Series of non–negative terms. The number e - The root and ratio tests.

Unit III

Power series – Summation by parts – Absolute convergence – Addition and Multiplication of series – Rearrangements

Unit IV

Continuity: Limits of functions – Continuous functions, Continuity and Compactness, Continuity and Connectedness – Discontinuities – Monotonic functions – infinite limits and limits at infinity.

Unit V

Text Book

Walter Rudin, Principles of Mathematical Analysis, III Edition (Relevant portions of chapters II, III, IV & V), McGraw-Hill Book Company, 1976.

Books for Supplementary Reading and Reference:

- 1. H.L.Royden, Real Analysis, Macmillan Publ.co., Inc. 4th edition, New York, 1993.
- 2. V.Ganapathy Iyer, Mathematical Analysis, Tata McGraw Hill, New Delhi, 1970.
- 3. T.M.Apostal, Mathematical Analysis, Narosa Publ. House, New Delhi, 1985.

CORE COURSE-III – DIFFERENTIAL GEOMETRY

Unit I

Space Curves – Definition of a space Curve – Arc length – tangent – normal and binormal – Curvature and Torsion – Contact between Curves and Surfaces – tangent surface – Involutes and evolutes – Intrinsic equations – Fundamental Existence Theorem for space Curves - Helices.

Unit II

Intrinsic Properties of a Surface – Definition of a Surface – Curves on a Surface – Surface of revolution – Helicoids – Metric – Direction Coefficients – families of Curves – Isometric Correspondence – Intrinsic properties.

Unit III

Geodesics – Canonical geodesic equations – Normal property of geodesics – Existence Theorems – Geodesic parallels.

Unit IV

Geodesic Curvature – Gaurs – Bonnet Theorem – Gaussian Curvature – Surface of Constant Curvature.

Unit V

Non-Intrinsic Properties of a Surface – The second fundamental form – Principal Curvature – Lines of Curvature – Developable – Developable associated with space curves and with curves on surfaces.

Text Book

T.J.Willmore, An Introduction to Differential Geometry, Oxford University Press (17th Impression) New Delhi 2002 (Indian Print)

Chapter I	:	Sections 1 to 9
Chapter II	:	Sections 1 to 9
Chapter II	:	Sections 10 to 14
Chapter II	:	Sections 15 to 18
Chapter III	:	Sections 1 to 6

Books for Supplementary Reading and Reference:

- 1. D.Somasundaram, Differential Geometry, A First Course, Narosa Publishing House, Chennai, 2005.
- 2. D.J.Struik, Classical Differential Geometry, Addison Wesley Publishing Company INC, Massachusetts, 1961.

```
******
```

CORE COURSE-IV – ORDINARY DIFFERENTIAL EQUATIONS Unit I

Linear equations with constant coefficients – Linear dependence and Independence – a formula for the Wronskian – non-homogenous equation – homogeneous equation of order n-initial value problems for n^{th} order equations – equations with real constants – non-homogeneous equations of order n.

Unit II

Linear equations with variable coefficients : Reduction of the order of a homogeneous equation – non-homogeneous equation-homogeneous equations with analytic coefficients – Legendre equation.

Unit III

Linear equations with regular singular points – Euler equations – second order equations with regular singular points – an example – second order equations with regular singular points – general case – exceptional cases – Bessel equation – Bessel equation (continued) – regular points at infinity.

Unit IV

Existence and uniqueness of solutions to first order equations : Equations with variables separated – exact equations – method of successive approximations – Lipchitz condition – convergence of the successive approximations.

Unit V

Nonlocal existence of solutions-approximations to solutions and uniqueness of solutions – Existence and uniqueness of solutions to systems and n^{th} order equations – existence and uniqueness of solutions to system.

Text Book

Earl A.Coddington, An Introduction to Ordinary Differential Equations – Prentice Hall of India, 1987.

Unit – I Chapter - 2 sections 2.4 to 2.10

- Unit II Chapter 3 sections 3.5 to 3.8
- Unit III Chapter 4 sections 4.1 to 4.4 and 4.6 to 4.9
- Unit IV Chapter 5 sections 5.2 to 5.6
- Unit -V Chapter 5 & 6 sections 5.7 to 5.8 and 6.6

Books for Supplementary Reading and Reference:

- 1. D.Somasundaram, Ordinary Differential Equations, Narosa Publishing House, Chennai, 2002.
- 2. M.D.Raisinghania, Advanced Differential Equations, S.Chand and Company Ltd, New Delhi, 2001.

ELECTIVE COURSE-I (A) – NUMBER THEORY

Unit I

The fundamental Theorem of Arithmetic: Introduction – divisibility – greatest common divisor – Prime Numbers – The Fundamental theorem of arithmetic – The series of reciprocals of the primes the Euclidean Algorithm – the greatest common divisors of more than two numbers.

Unit II

Arithmetical functions and Dirichlet Multiplication: Introduction; the Mobius function $\mu(n) - \theta$ and μ – product formula for $\theta(n)$ the Dirichlet product of arithmetical functions Dirichlet inverses and the mobius inversion formula the Mangoldt function Λ (n) – Multiplicative functions – Multiplicative functions; and Dirichlet multiplication – the inverse of a Completely multiplicative function – Liouville's fn λ (n) – the division functions $\sigma\alpha$ (n) – Generalized Convolutions – Formal Power Series – the Bell series of an arithmetical function Bell series and Dirichlet Multiplication – Derivatives of arithmetical functions the selberg identity.

Unit III

Averages of Arithmetical Functions: Introduction The big on notation Asymptotic equality of functions – euler's summation formula some elementary asymptotic formulas – the average order of d (n) – the average order of the division functions $\sigma \pounds(n)$ – the average order of Ψ (n) an application to the distribution of lattice points. Visible from the origin the average order μ (n) and of Λ (n) the partial sums of a Dirichlet product – Applications to $\mu(n)$ and Λ (n) Another identity for the partial sums of a Dirichlet product.

Unit IV

Congruences: Definition and Basic properties of congruences Residue classes and complete residue systems linear congruences – reduced residue systems and the Euler – Fermat theorem– Polynomial congruences modulo Lagrange's theorem – Applications of Lagrange's theorem Simultaneous linear congruences the Chinese remainder theorem – Application of the Chinese remainder theorem – polynomial congruences with prime power moduli the principle of cross classification a decomposition property of reduced residue systems.

Unit V

Quadratic residuces and the Quadratic Reciprocity Law: Lagrange's symbol and its properties– evaluation of (-1/p) and (2/P) – Gauss's Lemma – the quadratic reciprocity law applications of the reciprocity law the Jacobi symbol applications to Diophantine Equations.

Text Book

Tom M. Apostal, Introduction to Analytic Number theory, Springer Verlag.

Chapters : I, II, III, V & IX (upto Diophantine equations)

Books for Supplementary Reading and Reference:

- 1. Niven and H.S.Zuckerman, An Introduction to the Theory of Numbers, 3rd Edition, Wiley Eastern Ltd., New Delhi, 1989.
- 2. D.M.Burton, Elementary Number Theory, Universal Book Stall, New Delhi, 2001.

******** I YEAR – I SEMESTER

COURSE CODE: 7MMA1E2

ELECTIVE COURSE-I (B) – CALCULUS OF VARIATIONS AND SPECIAL FUNCTIONS

Unit I

Functional – The fundamental lemma – Euler's equation – minimum surface of revolution – Brachistochrone problem – Problems on geodesics – isoperimetric problems.

Unit II

Several dependent variables – Functional dependent on Higher order Derivative – Functionals dependent variables – Variational problems – Parametric form

Unit III

Hamiltous' Principle – Lagrange's equations – Problems on vibrations – Direct methods in variational problems – Euler's finite difference method – Ritz method and Kantorovich's method problems.

Unit IV

Legendre functions – Legendre Polynomials – Recurrence formula – Rodrigue's formula – properties – Bessel functions – Gamma function – recurrence formula – generating function – properties of Bessel functions.

Unit V

Hermite, Legendre and chebyshev functions and polynomials – Generating functions – Properties.

Text Books

- 1) L.Elsgolts, Differential Equations & Calculus of Variations, Mir Publishers(Units I, II & III)
- 2) G.F.Simmons, Differential Equations with Applications and Historical Notes, Tata McGraw Hill, New Delhi, (Units IV & V)

Books for Supplementary Reading and Reference:

- 1) Advanced Mathematics for Engineering and Science by M.K. Venkataraman, National Publishing Company Pvt. Ltd.
- 2) Methods of Applied Mathematics by F.B.Hildebrand, PHI.
- 3) Advanced Engineering Mathematics by Erwin Kreyzig, Wiley Eastern.
- 4) Differential Equations with Special Functions by Sharma and Gupta, Krishna Prakasan Mandir.
- 5) Higher Engineering Mathematics by B.S.Grewal, Kanna Publishers.

******** I YEAR – I SEMESTER

COURSE CODE: 7MMA1E3

ELECTIVE COURSE-I (C) – DATA STRUCTURES AND ALGORITHMS THEORY AND PRACTICAL

Unit I

Preliminaries in C++: Functions and Parameters Dynamic Memory Allocation – Classes – Testing and Debugging Programming Performances: Space Complexity – Time Complexity – Asymptotic Notation (O, Ω , θ , o) Practical Complexity – Performance Measurements.

Unit II

Data Representation: Linear Lists – Formula based representation – Linked representation – Indirect Addressing – Simulating Pointers – Applications. Arrays Matrices: Arrays – Matrices – Special Matrices – Sparse Matrices. Stacks and Queues: The Abstract Data Type – Derived Classes and Inheritance – Formula based Representation – Linked Representation – Applications – Hashing.

Unit III

Binary and other Trees: Trees – Binary Trees – Properties of binary trees – Representation of Binary Trees – Common Binary tree operations – Binary Tree traversal – The ADT Binary tree – Applications – Priority Queues: Linear Lists – Hash – Leftist Trees – Applications – Search Trees – AVL Trees – B-Trees – Applications – Graphs.

Unit IV

The Greedy Method: Optimization Problems – Greedy Method – Applications Divide and Conquer: The Method – Applications – Lower Bounds on Complexity.

Unit V

Dynamic Programming: The Method – Applications – Backtracking – The Method – Applications – Branch and Bound: The Method – Applications.

Text Book

SAHNI, Data structures, Algorithms and Applications in C++ – International Edition 1998, Tata McGraw Hill.

DATA STRUCTURES AND ALGORITHMS IN C++ LAB

- 1. Stack implementation using Arrays and Linked List
- 2. Queue implementation using Arrays and Linked List
- 3. Binary Search Tree
- 4. Single Linked List, Doubly Linked and Circular Linked List
- 5. Different Types of Sorting (Quick, Bubble, Merge etc)
- 6. String Operations
- 7. Number Generation (Prime Number, Fibonacci, Armstrong, Perfect Numbers)
- 8. Searching (Linear and Binary)
- 9. SPARSE Matrix
- 10. Polynomial Addition
- 11. Tree Traversal
- 12. Sum of Alternate Digits
- 13. Student File (Mark Processing)
- 14. Matrix Multiplication
- 15. Employee Details

I YEAR–II SEMESTER COURSE CODE: 7MMA2C1

CORE COURSE-V-ALGEBRA-II

Unit I

Vector Space: Elementary basic concepts - Linear Independence and Basis.

Unit II

Dual spaces – Inner product spaces.

Unit III

Field: Extension fields – Roots of polynomials – More about roots.

Unit IV

The Elements of Galois theory.

Unit V

Linear Transformations: The Algebra of linear transformations – Characteristic roots – Matrices – Canonical forms Triangular Form – Hermitian, Unitary, and Normal transformations.

Text Book

I.N.Herstein, Topics in Algebra (2nd edition) John Wiley and Sons, New York.

Chapter IV	:	(Sections 4.1 to 4.4)
Chapter V	:	(Sections 5.1, 5.3, 5.5, 5.6)
Chapter VI	:	(Sections 6.1, 6.2, 6.3, 6.4, and 6.10)

Books for Supplementary Reading and Reference:

- 1. P.B.Bhattacharya, S.K.Jain and S.R.Nagpaul, Basic Abstract Algebra (2nd edition) Cambridge University Press, 1997 (Indian Edition)
- 2. S.Lang, Algebra 3rd edition, Addison-Wesley, Mass, 1993.
- 3. N.Jacobson, Basic Algebra, Vol. I & II W.H.Freeman, also Published by Hindustan Publishing Company, New Delhi, 1980.

CORE COURSE-VI-ANALYSIS-II

Unit I

Riemann-Stieltjes Integral: Definition and Existence of the Integral – Properties of the Integral, Integration and Differentiation, Integration of vector – valued functions – Rectifiable curves.

Unit II

Sequences and Series of functions: Discussion of main problem, Uniform convergence – continuity- Integration and Differentiation, Equicontinuous families of functions – the Stone Weierstrass theorem.

Unit III

Some special functions: Power series, the Exponential, Logarithmic and Trigonometric functions – the Algebraic completeness of the Complex field – Fourier Series – The Gamma function.

Unit IV

Lebesgue measure: Algebra of sets – Measurable space – Lebesgue outer measure – Lebesgue measurable sets – non-measurable sets – Lebesgue measurable functions – Little wood's three principles.

Unit V

Lebesgue Integral: Riemann integral – Lebesgue Integral of a bounded function over a set of finite measure – Lebesgue Integral of nonnegative measurable function – general Lebesgue integral – Convergence theorems on measurable functions.

Text Book(s)

- 1. Walter Rudin, Principles of Mathematics Analysis (3rd edition), McGraw Hill 1976. (For Analysis part Chapters VI, VII and VIII)
- 2. H.L. Royden, Real Analysis (3rd edition) Macmillan Publishing Company, New York, 1988.(For Measure Theory chapters III and IV)

Books for Supplementary Reading and Reference:

- 1. G.De Barra, Measure Theory and Integration, Wiley Easten Ltd., New Delhi, 1987.
- 2. Malik S.C. and Savita Arora, Mathematical Analysis, Wiley Eastern Limited, New Delhi, 1991.

CORE COURSE-VII – PARTIAL DIFFERENTIAL EQUATIONS

Unit I

Ordinary differential equations in more than two variables : Surfaces and curves in three dimensions-simultaneous differential equations of the first order and the first degree in three variables-methods of solution of dx/P=dy/Q=dz/R orthogonal trajectories of a system of curves on a surface-pfaffian differential forms and equations – solution of Pfaffian differential equations the three variables.

Unit II

Partial differential equations of the first order : Partial differential equations – origins of first order partial differential equations – Cauchy's problem for first order equations – linear equations of the first order-integral surfaces passing through a given curve-surfaces orthogonal to a given system of surfaces-nonlinear partial differential equations of the first order-Cauchy's method of characteristics.

Unit III

Compatible systems of first order equations – Charpits method-special types of first order equations – solutions satisfying given conditions – Jacobi's method.

Unit IV

Partial differential equations of the second order : Origin of second order equations – linear partial differential equations with constant coefficients. Equations with variable coefficients – separation of variables – method of integral transforms (exercise problems are excluded)

Unit V

Laplace's equation : Elementary solutions of Laplace's equation – boundary value problems – The Wave equation – Elementary solutions of the one dimensional wave equation – The Diffusion equation : Elementary solutions of the diffusion equation – separation of variables.

Text Book(s)

- 1. I.N.Sneddon,Elements of Partial Differential Equations,McGraw Hill Book Company, 1986.
 - Unit I : Chapter 1 : Sections 1.1 to 1.6
 - Unit II : Chapter 2 : Sections 2.1 to 2.8
 - Unit III: Chapter 2 : Sections 2.9 to 2.13
 - Unit IV: Chapter 3 : Sections 3.1, 3.4, 3.5, 3.9 and 3.10
 - Unit V : Chapter 4, 5 & 6 : Sections 4.2, 4.4, 5.2, 6.3 and 6.4

Books for Supplementary Reading and Reference:

- 1. M.D.Raisinghania, Advanced Differential Equations, S.Chand&Company Ltd., New Delhi, 2001.
- 2. K.Sankara Rao, Introduction to Partial Differential Equations, Second Edition, Prentice Hall of India, New Delhi, 2006.
- 3. J.N.Sharma and K.Singh, Partial Differential Equations for Engineers and Scientists, Narosa Publishing House, Chennai, 2001.

CORE COURSE-VIII – MECHANICS

Unit I

 $The \ mechanical \ system-generalized \ coordinates-constraints-virtual \ work-energy \ and \ momentum.$

Unit II

Derivation of Lagrange's equations - examples - integrals of motion.

Unit III

Hamilton's principle – Hamilton's equations – other variations principle.

Unit IV

Hamilton principle function – Hamilton – Jacobi equations – separability.

Unit V

Differential forms and generation functions – special transformations – Lagrange and Poisson brackets.

Text Book(s)

1. D.Greenwood, Classical Dynamics, Prentice Hall of India, New Delhi, 1985.

Unit I :	Chapters 1 sections 1.1 to 1.5
Unit II :	Chapters 2 sections 2.1 to 2.3
Unit III:	Chapters 4 sections 4.1 to 4.3
Unit IV:	Chapters 5 sections 5.1 to 5.3
Unit V :	Chapters 6 sections 6.1 to 6.3

Books for Supplementary Reading and Reference:

- 1. H.Goldstein, Classical Mechanics, 2nd edition, Narosa Publishing House, New Delhi.
- 2. N.C.Rane and P.S.C Joag, Classical Mechanics, Tata McGraw Hill, New Delhi, 1991.
- 3. J.L.Synge and B.A.Griffth, Principles of Mechanics, McGraw Hill Book Co., New York, 1970.

ELECTIVE COURSE-II (A) – GRAPH THEORY

Unit I

Graphs – Subgraphs – Trees.

Unit II

Connectivity – Euler Tours and Hamiltonian cycles.

Unit III

Matchings – Edge colouring.

Unit IV

Independent sets and cliques - vertex colourings.

Unit V

Planar graphs.

Text Book

J.A.Bondy and V.S.R.Murty, Graph Theory and applications, Macmillan, London, 1976.

Chapter I	:	(Sections 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7)
Chapter II	:	(Sections 2.1, 2.2, 2.3, 2.4)
Chapter III	:	(Sections 3.1, 3.2)
Chapter IV	:	(Sections 4.1, 4.2)
Chapter V	:	(Sections 5.1, 5.2)
Chapter VI	:	(Sections 6.1, 6.2)
Chapter VII	:	(Sections 7.1, 7.2)
Chapter VIII	:	(Sections 8.1, 8.2)
Chapter IX	:	(Sections 9.1, 9.2, 9.3, 9.4 & 9.6)
-		

Books for Supplementary Reading and Reference:

- 1. S.A.Choudum, A First Course in Graph Theory, Macmillan, India Ltd., 1987.
- 2. R.Balakrishnan and K.Renganathan, A Text Book of Graph Theory, Springer Verlag, New York, 1999.

ELECTIVE COURSE-II (B) – APPLIED ALGEBRA

Unit I

Finite State Machines: Introduction – Binary Devices and States – Finite state Machines – Covering and equivalence – Equivalent States – A minimization procedures – Turing machines – Incompletely specified machines – Relations between states – a minimization procedure.

Unit II

Programming Languages: Introduction – Arithmetic expressions – Identifies: assignment statements – Arrays – FOR statements – Block structures in ALGOL – The ALGOL grammer– Evaluating arithmetic statements – compiling arithmetic expressions.

Unit III

Boolean Algebras: Introduction – Order – Boolean polynomials – Block diagrams for gating networks – connections with logic – logical capabilities of ALGOL – Boolean Applications – Boolean subalgebras – Disjunctive normal form – Direct Products; morphisms.

Unit IV

Optimization and computer Design: Introduction – optimization – Computerizing optimization – Logic design – NAND gates and NOR gates – The minimization problem – procedure for deriving prime implicants – consensus taking – Flip – Flops – Sequential machine design.

Unit V

Binary Group Codes: Introduction – Encoding and Decoding – Block codes Matrix encoding techniques – Group codes – Decoding tables – Hamming codes.

Text Book

Modern Applied Algebra by Garret Birkhoff and Thomas C.Bartee, McGraw Hill International Student Edition.

Chapters : III, IV, V, VI & VIII

ELECTIVE COURSE-II (C) – DIFFERENCE EQUATIONS

Unit I

Difference calculus – Difference Operator – Summation Generating function and Approximate Summation.

Unit II

Linear Difference Equations – First order equations – General results for linear equations – Solving Linear Equations.

Unit III

Equations with variable coefficients – The Z-Transform.

Unit IV

Stability Theory – Initial Value Problems for linear Systems – Stability of linear systems.

Unit V

Asymptotic Methods – Introduction – Asymptotic analysis of sums – linear equations.

Text Book

W.G.Kelley and A.C.Peterson, Difference Equations, 2nd edition, Academic Press, New York, 1991.

Chapter 2: Sections 2.1 - 2.3 Chapter 3: Sections 3.1, 3.3, 3.5 and 3.7 Chapter 4: Sections 4.1 and 4.2 Chapter 5: Sections 5.1 to 5.3

Books for Supplementary Reading and Reference:

- 1. S.N.Elaydi, An Introduction to Difference Equations, Springer Verlag, New York, 1995.
- 2. R.P.Agarwal, Difference Equations and Inequalities, Marcel Dekkar, New York, 1992.

CORE COURSE-IX-COMPLEX ANALYSIS

Unit I

Concept of analytic function – Elementary theory of power series – Conformability – Linear transformations.

Unit II

Complex integration – Cauchy integral formula.

Unit III

Local properties of analytic functions.

Unit IV

Calculus of residues.

Unit V

Power series expansions - canonical products - Jensen's formula.

Text Book

Lars V.Ahlfors, Complex Analysis, 3rd edition, McGraw Hill International Book Company, 1979.

Chapter II	:	(Sections 1, 2)
Chapter III	:	(Sections 2, 3)
Chapter IV	:	(Sections 1, 2, 3, & 5)
Chapter V	:	(Sections 1.1, 1.2, 1.3, 2.1, 2.2, 2.3, 3.3).

Books for Supplementary Reading and Reference:

- 1. S.Ponnusamy, Foundations of Complex Analysis, Narosa Publication House, New Delhi, 2004.
- 2. John B.Conway, Functions of One Complex Variable, 2nd edition, Springer-Verlag, International Student Edition, Narosa Publishing Company.

CORE COURSE-X-TOPOLOGY – I

Unit I

Topological Spaces – Basis of a topology – the order topology – the product topology on XxY – the subspace topology – closed sets and limit points.

Unit II

Continuous functions – the product topology – the metric topology – the quotient topology.

Unit III

Connected spaces – connected sets in the real line – components and path components – local connectedness.

Unit IV

Compact spaces – compact sets in the real line – limit point compactness.

Unit V

The countability axioms – the separation axioms – the Urysohn's lemma – the Uryshon's metrization theorem.

Text Book

James R.Munkres, Topology a first course, Prentice Hall of India Pvt. Ltd., New Delhi (1987)

:	(Sections 2.1 to 2.10)
:	(Sections 3.1 to 3.4)
:	(Sections 3.5 to 3.7)
:	(Sections 4.1 to 4.4)
	: : :

Books for Supplementary Reading and Reference:

- 1. James Dugundji, Topology, Prentice Hall of India, New Delhi, 1975.
- 2. George F.Simmons, Introduction to Topology and Modern Analysis, McGraw Hill Book Co., 1963.

CORE COURSE-XI – PROBABILITY AND STATISTICS

Unit I

Probability and Distribution: Introduction – Set theory – The probability set function – Conditional probability and independence – Random variables of the discrete type – Random variables of the continuous type – properties of the distribution function – expectation of random variable – some special expectations – Chebyshev's Inequality.

Unit II

Multivariate Distributions: Distributions of two random variables – Conditional Distributions and Expectations – the correlation coefficient – Independent random variables – extension to several Random variables.

Unit III

Some special Distributions: The Binomial and Related Distributions – The Poisson Distribution– The Gamma and Chi-square Distributions – The Normal Distribution – The Bivariate Normal Distribution.

Unit IV

Distributions of functions of Random variables: Sampling Theory – Transformations of variables of the discrete type – Transformations of variables of the continuous type – the Beta, t and F distributions – Extensions of the change – of – variable Technique –Distributions of order statistics – The Moment generating – Function, Techniques – The distributions of X and ns^2/σ^2 – Expectations of functions of Random variables

Unit V

Limiting Distributions : Convergence in distribution – convergence in probability – Limiting Moment Generating Functions – The Central Limit Theorem – Some theorems on Limiting Distributions.

Text Book:

1. Introduction to Mathematical Statistics, (Fifth edition) by Robert V.Hogg and AllenT. Craig Pearson Education Asia.

Chapters I, II, III, IV (Omit 4.10) & V. **Books for Supplementary Reading and Reference:**

- 1. M.Fisz, Probability, Theory and Mathematical Statistics, John Wiley and Sons, New York. 1963.
- V.K.Rohatgi, An Introduction to Probability Theory and Mathematical Statistics, Wiley Eastern Ltd., New Delhi, 1988 (3rd Print)

ELECTIVE COURSE-III (A) – DISCRETE MATHEMATICS

Unit I

Algebraic Systems : Binary Operation – Algebraic Systems – Semigroups and Monoids – Homorphism and Isomophism of Semigroups and Monoids – Properties of Homomorphism – Subsemi groups and Submonoids.

Unit II

Mathematical Induction – Techniques of Proof – Mathematical Induction – Recurrence Relations and Generating Functions – Recurrence – an introduction – Polynomials and their Evaluations Recurrence Relations – Solution of Finite order Homogeneous (Linear) Relations.

Unit III

Solution of Non-homogeneous Relations – Generations Functions – Some Common Recurrence Relations – Primitive Recursive Functions – Recursive and Partial Recursive Fnctions.

Unit IV

 $Lattices-Lattices-Some\ Properties\ of\ Lattices-New\ Lattices-Modular\ and\ Distributive\ Lattices.$

Unit V

Boolean Algebra – Boolean Algebras – Boolean Polynomials – Karnaugh Map – Switching Circuits

Text Book:

1. Dr. M.K.Venkataraman, Dr. N.Sridharan and Dr. N.Chandra Sekaran, The National Publishing Company, Chennai.

Chapter IV; Chapter V -Sections 1 to 9 Chapter VII -Sections 7.1 to 7.6; Chapter X

Books for Supplementary Reading and Reference:

- 1. Rudolf Lidl and Gunter Pilz, Applied Abstract Algebra, 2nd Indian Reprint 2006, Springer Verlag, New York.
- 2. Kenneth H. Rosen, Discrete Mathematics and its Applications, Fourth edition, McGraw Hill Publications.
- 3. A.Gill, Applied Algebra for Computer Science, Prentice Hall Inc., New Jersey.

ELECTIVE COURSE-III (B) – FLUID DYNAMICS

Unit I Kinematics of fluids in motion

Real fluids and Ideal fluids - Velocity of a fluid at a point - Stream lines and path lines - Steady and Unsteady flows – The Velocity Potential - The Vorticity Vector - Local and Particle Rates of Change – The equation of Continuity - Worked Examples - Acceleration of a Fluid.

Unit II Equations of Motion of a Fluid

Pressure at a point in a fluid at rest - Pressure at a point in a moving fluid - Euler's equations of Motion - Bernoulli's equation - Worked Examples - Discussion of the case of steady motion under Conservative Body Forces -Some flows involving axial symmetry.

Unit III Some Three-Dimensional Flows

Introduction - Sources, Sinks and Doublets Images in rigid infinite plane - Images in solid spheres - Axis symmetric flows - Stoke's Stream Function.

Unit IV Some Two-Dimensional Flows

The Stream Function - The Complex Velocity Potential for Two - Dimensional Irrotational, Incompressible Flow - Complex Velocity - Potentials for Standard Two-Dimensional Flows - Some Worked - Examples - Two Dimensional Image Systems - The Milne-Thomson - Circle Theorem.

Unit V Viscous Fluid

Stress components in a real fluid - Relation between Cartesian - Components of Stress - Translational motion of fluid element – The Coefficient of Viscosity and Laminar flow - The Navier-Stokes equation of a viscous fluid - Some solvable problems in viscous flow - Steady motion between parallel planes only.

Text Book

1. Frank Chorlton, Textbook of Fluid Dynamics, CBS Publishers & Distributors, 2004.

Chapter 2: Sections 2. - 2.9 Chapter 3: Sections 3.1, 3.2, 3.4 - 3.7, 3.9 Chapter 4: Sections 4.1 - 4.5 Chapter 5: Sections 5.3-5.8 Chapter 8: Sections 8.1-8.3, 8.8, 8.9, 8.10.1

Books for Supplementary Reading and Reference:

- 1. E.Karuse, Fluid Mechanics with Problems and Solutions, Springer, 2005.
- 2. R.W.Fox and A.T.McDonald, Introduction to Fluid Mechanics, Wiley, 1985.

ELECTIVE COURSE-III (C) – AUTOMATA THEORY

Unit I

Definition of automata – transition system – acceptability of a string by finite automation –Non – deterministic finite state machines – the equivalence of DFA and NDFA.

Unit II

Formal languages – Chomsky classification of languages – Languages and their relations.

Unit III

 $\label{eq:cursive} Recursive and Recursively Enumerable sets - Operation on languages - Languages and Automata.$

Unit IV

Regular expressions – finite Automata and regular expansions – Pumping Lemma for regular sub–closure properties of regular sets.

Unit V

Context – Free languages – simplication of context free Grammar – Normal forms for context free languages.

Text Book

K.L.P.Mishra and N. Chandrasekaran, Theory of Computer Science, (Automata, Languages and Computation) III Edition, Prentice Hall of India (2007).

Chapter III	:	(Sections 3.1 to 3.7)
Chapter IV	:	(Sections 4.1 to 4.6)
Chapter V	:	(Sections 5.1 to 5.5)
Chapter VI	:	(Sections 6.1 to 6.4)

Books for Supplementary Reading and Reference:

- 1. John E.Hopcroft, Rajeev Motwanl, Jeffrey D.Ullmon, Introduction to Automata Theory, Langauges and Computation, 3rd edition, Pearson Addison Wesley.
- 2. Harry R.Lewis and Christos H. Papadimitriou, Elements of the Theory of Computation, 2nd edition, Prentice Hall, 1997.

ELECTIVE COURSE- IV- (A) – FUZZY MATHEMATICS

Unit I

Crisp sets and fuzzy sets.

Unit II

Operation on fuzzy sets.

Unit III

Fuzzy relations.

Unit IV

Fuzzy measures.

Unit V

Uncertainty and Information.

Text Books

1. J.Klir and Tina A Folger, Fizzy Sets, Uncertainty and Information, Prentice Hall of India Private Ltd., New Delhi, 2006

Chapters : I, II, III, IV and V upto section 5.5.

Books for Supplementary Reading and Reference:

- 1. V.Novak, Fuzzy Sets and Their Applications, Adom Hilger, Bristol, 1969.
- 2. A.Kaufman, Introduction to the Theory of Fuzzy Subsets, Academic Press, 1975.
- 3. H.J.Zimmermann, Fuzzy Set Theory and its Applications, Allied Publishers, Chennai, 1996.

ELECTIVE COURSE IV (B) – STOCHASTIC PROCESSES

Unit I

Stochastic Processes: Basic concepts - Markov chains.

Unit II

Definition, Transition Matrix, order of Markov chain, Higher Transition probabilities – classifications of states and chains, Determinations of Higher transition probabilities.

Unit III

Stability of a Markov chain, Limiting behaviour Markov process and related distributions.

Unit IV

Generalizations of Poisson process. Birth and death process, Markov processes.

Unit V

Renewal processes: Renewal Equations, Renewal Theorems, delayed and equilibrium renewal processes, residual and excess life times.

Text Book

J. Medhi, Stochastic Processes, 2nd edition, Wiley Eastern, June 1987

Chapter II	:	Full
Chapter III	:	(Sections 3.1, 3.2, 3.3, 3.4, 3.5)
Chapter IV	:	(Sections 4.1, 4.2, 4.3, 4.4, 4.5)
Chapter VI	:	(Sections 6.1, 6.2, 6.3, 6.4, 6.5)

Books for Supplementary Reading and Reference:

- 1. S.K.Srinivasan and A.Vijayakumar, Stochastic Processes, Narosa, 2003.
- 2. E.Cinlar, Introduction to Stochastic Processes, Prentice Hall of India, 1975.

ELECTIVE COURSE-IV (C) – COMBINATORIAL MATHEMATICS

Unit I

Generating function.

Unit II

Recurrence relation.

Unit III

The principle of inclusion and exclusion.

Unit IV

Polya theory of counting.

Unit V

Block Designs.

Text Book

CL.Liu, Introduction to Combinatorial Mathematics, Tata McGraw Hill.

Chapters : II III, IV, V & XIV.

Books for Supplementary Reading and Reference:

- 1. R.P.Stanley, Enumerative Combinatorics, Volume I, Cambridge Studies in Advanced Mathematics, Volume 49, Cambridge University Press, 1997.
- 2. P.J.Cameron, Combinatorics : Topics, Techniques, Algorithms, Cambridge University Press, Cambridge, 1998.

CORE COURSE-XII –FUNCTIONAL ANALYSIS

Unit I

Normed spaces, continuity of linear Maps.

Unit II

Hahn – Banach theorems, Banach limits, Banach spaces.

Unit III

Uniform boundedness Principle - Closed graph and open mapping theorems

Unit IV

Duals and Transposes, Duals of L^p ([a, b]) and C ([a, b]) (excluding moment sequences)

Unit V

Inner product spaces, orthonormal sets, projection and Reisz Representation theorems.

Text Book

Functional Analysis by B.V Limaye, Second Edition, New Age International Pvt. Ltd., Publishers.

Chapter II	:	(Section 5, 6, 7, 8)
Chapter III	:	Section 9 (Subsections 9.1, 9.2, & 9.3 only)
		& Sections 10
Chapter IV	:	(Sections 13, 14)
		(excluding Moment Sequences Subsections 14.6
		& 14.7)
Chapter VI	:	(Sections 21, 22, and 24.1, 24.2, 24.3 & 24.4)

Books for Supplementary Reading and Reference:

- 1. G.F.Simmons, Introduction to Topology and Modern Analysis, Tata McGraw Hill Publishing Company, New Delhi, 2004.
- 2. H.C.Goffman and G.Fedrick, First Course in Functional Analysis, Prentice Hall of India, New Delhi, 1987.
- 3. Walter Rudin, Functional Analysis, Tata McGraw Hill Publishing Company, New Delhi, 1973.

CORE COURSE XIII – OPERATIONS RESEARCH

Unit I

Network Models: Scope and definition of network models – Minimal spanning tree algorithm– Shortest – Route Problem: Examples of the shortest route applications, Shortest route algorithms, linear programming formulation of the shortest route problem – maximal flow model – Enumeration of cuts, maximal flow algorithm, linear programming formulation of maximal flow mode – CPM and PERT: Network representation, CPM Computations, construction of the time schedule, Linear programming formulation of CPM, PERT calculations.

Unit II

Deterministic inventory Models: General inventory Model – role of demand in the development of inventory models – static Economic – Order – Quantity models – Classic EOQ model, EOQ with price breaks, Multi item EOQ with storage limitation – Dynamic EOQ models: No setup Model, Setup Model.

Unit III

Queing systems: Elements of a queuing model – Role of exponential distribution – Pure birth and Death Models (relationship between the Exponential and Poisson distributions) Pure birth Model, Pure death model.

Unit IV

Generalized poisson queuing model Specialized poisson Queues: Steady State measures of performance, Single Server Models, multiple server models, Machine Servicing Model (M/M/R): (GD/K/K), R>K – (M/G/1): (GD/ ∞/∞) – Pollaczek – Khintchine (P-K) formula – other queuing Models, Queuing Decision Models.

Unit V

Non Linear Programming Algorithms: Unconstrained algorithms: Direct search Method, Gradient Method – Constrained Algorithms separable programming.

Text Book

Hamdy A.Taha, Operations Research, An Introduction (8th edition), Prentice – Hall of India Pvt. Ltd., New Delhi.

Chapters : VI, XI, XV and XIX (upto 19.2.1)

Books for Supplementary Reading and Reference:

- 1. J.K.Sharma, Operations Research, Theory and Applications, 3rd edition, Macmillan India Ltd, 2007.
- 2. F.S.Hillier and G.J.Lieberman, Introduction to Operations Research (8th edition) Tata McGraw Hill Publishing Company, New Delhi, 2006.

CORE COURSE-XIV- TOPOLOGY - II

Unit I

Connectedness and Compactness: Local Compactness – The Tychonoff Theorem: The Tychonoff theorem.

Unit II

Completely Regular Spaces, The Stone – Cech Compactification.

Unit III

Metrization theorems and Paracompactness: Local Finiteness, The Nagata – Smirnov Metrization Theorem (Sufficiency) – The Nagata – Smirnov Theorem (necessity).

Unit IV

Complete Metric Spaces and Function Spaces: Complete metric spaces – A Space – Filling Curve – Compactness in Metric spaces – Point wise and compact convergence.

Unit V

The Compact – Open Topology – Ascoli's theorem – Baire Spaces – A Nowhere differentiable functions.

Text Book

James R Munkres, Topology, A First Course, Prentice Hall of India, New Delhi (1984)

Chapter III	:	(Section 3.8)
Chapter V	:	(Sections 5.1, 5.2, 5.3)
Chapter VI	:	(Sections 6.1, 6.2, 6.3)
Chapter VII	:	(Sections 7.1, 7.2, 7.3, 7.4, 7.5, 7.6, 7.7, 7.8)

Books for Supplementary Reading and Reference:

- 1. JL.Kelley, General Topology, Van Nostrnad, Reinhold Co., New York.
- 2. K.D.Joshi, Introduction to General Topology, Wiley Eastern Ltd., 1983.

ELECTIVE COURSE-V (A) – ADVANCED STATISTICS

Unit I

Introduction to statistical Inference: Point estimation – confidence intervals for means – confidence intervals for differences of means – test of statistical hypothesis – Additional comments about statistical tests – Chi-Square tests.

Unit II

Sufficient Statistics: Measures of Quality of Estimators – a sufficient statistic for a parameter– properties of a sufficient statistic – completiness and uniqueness the exponential class of probability density – functions of a parameter.

Unit III

More about estimation: Bayesian Estimation – Fisher Information and the Rao – Cramer inequality Limiting Distributions of Maximum Likelihood estimators.

Unit IV

Theory of statistical tests: Certain Best tests – Uniformly most powerful tests – Likelihood Ratio Tests – the sequential probability Ratio Test.

Unit V

Inferences about Normal Models: The distributions of certain Quadratic forms – A test of the equality of several means – Noncentral χ^2 and noncentral F – multiple comparisons – The analysis of variance – A regression problem – A test of independence.

Text Book

Robert V. Hogg and Allen T.Craig, Introduction to Mathematical Statistics (Fifth Edition) by Pearson Education, Asia.

Chapter	:	VI
Chapter	:	VII (Omit 7.7, 7.8 and 7.9)
Chapter	:	VIII (Omit 8.4)
Chapter	:	IX (Omit 9.5)
Chapter	:	X (Omit 10.8 and 10.9)

Books for Supplementary Reading and Reference:

- V.K.Rohatgi, An Introduction to Probability Theory and Mathematical Statistics, Wiley Eastern Ltd., New Delhi, 1998 (3rd Print)
- 2. M.Fisz, Probability Theory and Mathematical Statistics, John Wiley and Sons, New York, 1963.

ELECTIVE COURSE -V-(B) - STOCHASTIC DIFFERENTIAL EQUATIONS

Unit I

Probability spaces – Random variable and stochastic Processes – An Important Example – Brownian motion – Construction of the Ito Integral – Some properties of the Ito Integral – Extensions of the Ito Integral.

Unit II

The 1 – Dimensional Ito Formula – The Multi – Dimensional Ito Formula – The Martingale Representation Theorem.

Unit III

Stochastic Differential Equations – Examples and Some Solution Methods – An Existence and Uniqueness Result – Weak and Strong Solutions.

Unit IV

The Filtering Problem – Introduction – The 1 – Dimensional Linear Filtering Problem – The Multidimensional Linear Filtering Problem.

Unit V

Diffusions – Basic properties – The Markov Property – The Strong Morkov Property – The Generator of an Ito Diffusion – The Dynkin Formula – The characteristic operator.

Text Book

B.Oksendal, Stochastic Differential Equations : An Introduction with Applications, Sixth Edition, Springer – Verlag, Heidelberg, 2003.

Chapter 2 : Sections 2.1,2.2 Chapter 3 : Sections 3.1 - 3.3 Chapter 4 : Sections 4.1 - 4.3 Chapter 5 : Sections 5.1 - 5.3 Chapter 6 : Sections 6.1 - 6.3 Chapter 7 : Sections 7.1 - 7.5

Books for Supplementary Reading and Reference:

- 1. Avner Friedman, Stochastic Differential Equations and Applications, Dover Publications, 2006.
- 2. Ludwig Arnold, Stochastic Differential Equations, Theory and Applications, Dover Publications, 2011.

ELECTIVE COURSE-V (C)-NUMERICAL METHODS

Unit I

Transcendental and polynomial equations : Rate of convergence of iterative methods – Methods for finding complex roots – Polynomial equations – Birge – Vieta method, Bairstow's method, Graeffe's root squaring method.

Unit II

System of Linear Algebraic equations and Eigen Value Problems : Error Analysis of direct and iteration methods – Finding eigen values and eigen vectors – Jacobi and Power methods.

Unit III

Interpolation and Approximation : Hermite Interpolations – Piecewise and Spline Interpolation – Bivariate Interpolation – Approximation – Least square approximation and best approximations.

Unit IV

Differentiation and Integration : Numerical Differentiation – Optimum choice of Step – length – Extrapolation methods – Partial Differentiation – Methods based on undetermined coefficient – Gauss methods.

Unit V

Ordinary differential equations : Local truncation error – Euler, Backward Euler, Midpoint, Taylor's Method and second order Runge – Kutta method – Stability analysis.

Text Book

M.K.Jain, S.R.K.Iyengar and R.K.Jain, Numerical Methods for Scientific and Engineering Computation, III Edn. Wiley Eastern Ltd., 993.

Unit I - Chapter 2, 2.5 to 2.8 Unit II - Chapter 3, 3.3, 3.4, 3.5 Unit III - Chapter 4, 4.5 to 4.9 Unit IV - Chapter 5, 5.2, 5.3, 5.4, 5.5, 5.8 Unit V - Chapter 6, 6.2, 6.3, 6.6

Books for Supplementary Reading and Reference:

- 1. Kendall E.Atkinson, An Introduction to Numerical Analysis, II Edn., John Wiley & Sons, 1983.
- 2. M.K.Jain, Numerical Solution of Differential Equations, II Edn., New Age International Pvt Ltd., 1983.
- 3. Samuel, D. Conte, Carl. De Boor, Elementary Numerical Analysis, McGraw Hill International Edn., 1983.
